

FIG. 1



Start

Label primitive subexpressions of  $\Phi$  with spanning intervals that represent the sets of intervals over which the corresponding primitive event types hold

Are there any subexpressions that have not been labeled with sets of spanning intervals?

Let  $\Phi'$  be some subexpression of  $\Phi$  such that  $\Phi'$  is not labeled with sets of spanning intervals but for which all subexpressions  $\Phi_1^m$ ,...,  $\Phi_n^m$  of  $\Phi'$  are labeled with sets of spanning intervals

FIG. 2

Apply the appropriate formula for  $\varepsilon(M,\Phi')$  using the subroutines  $\langle i \rangle$ ,  $i_1 \cap i_2, \neg i$ , SPAN  $(i_1,i_2), \mathfrak{D}(r,i)$ , and  $\mathcal{I}(i,r,j)$  to compute a set of spanning intervals to label  $\Phi'$ 



```
x = y \triangleq \overline{x = y}
SUPPORTED(x) \triangleq \overline{\neg GROUNDED(x)}
RIGIDLYATTACHED(x, y) \triangleq (\exists r)RIGID(x, y, r)
SUPPORTS(x, y) \triangleq \left( \overline{\neg GROUNDED(y) \land} \\ \neg STABLE(P \setminus \{x\}, M \cup \{GROUNDED(z) | \neg RIGIDLYATTACHED^*(z, y)\}) \right)
CONTACTS(x, y) \triangleq \overline{TOUCHES(x, y) \land x \bowtie y}
ATTACHED(x, y) \triangleq \overline{(\exists r)RIGID(x, y, r) \lor REVOLUTE(x, y, r)}
```

FIG. 3



```
\neg \Diamond x = y \land \neg \Diamond z = x \land \neg \Diamond z = y \land
                                                        Supported(y) \land \neg \Diamond Attached(x, z) \land
                                                                  \neg \Diamond \mathsf{ATTACHED}(x,y) \land \neg \Diamond \mathsf{SUPPORTS}(x,y) \land
                                                                  SUPPORTS(z, y) \land
                                                                  \neg \Diamond \text{SUPPORTED}(x) \land \neg \Diamond \text{ATTACHED}(y, z) \land
                                                                  \neg \Diamond \text{SUPPORTS}(y, x) \land \neg \Diamond \text{SUPPORTS}(y, z) \land
              PICKUP(x, y, z) \stackrel{\triangle}{=}
                                                                  \neg \Diamond \text{SUPPORTS}(x, z) \land \neg \Diamond \text{SUPPORTS}(z, x)
                                                              [ATTACHED(x, y) \lor ATTACHED(y, z)];
                                                                  Attached(x, y) \land Supports(x, y) \land
                                                                  \neg \Diamond \text{SUPPORTS}(z, y) \land
                                                                  \neg \Diamond \text{SUPPORTED}(x) \land \neg \Diamond \text{ATTACHED}(y, z) \land
                                                                  \neg \Diamond \text{SUPPORTS}(y, x) \land \neg \Diamond \text{SUPPORTS}(y, z) \land
                                                                  \neg \Diamond \text{SUPPORTS}(x, z) \land \neg \Diamond \text{SUPPORTS}(z, x)
                                                        \neg \Diamond x = y \land \neg \Diamond z = x \land \neg \Diamond z = y \land
                                                        SUPPORTED(y) \land \neg \Diamond ATTACHED(x, z) \land
                                                                  Attached(x, y) \land Supports(x, y) \land
                                                                  \neg \Diamond \text{SUPPORTS}(z, y) \land
                                                                  \neg \Diamond \text{SUPPORTED}(x) \land \neg \Diamond \text{ATTACHED}(y, z) \land
                                                                  \neg \Diamond \text{SUPPORTS}(y, x) \land \neg \Diamond \text{SUPPORTS}(y, z) \land
         PutDown(x, y, z) \stackrel{\triangle}{=}
                                                                 \neg \Diamond \text{SUPPORTS}(x, z) \land \neg \Diamond \text{SUPPORTS}(z, x)
                                                              [ATTACHED(x, y) \lor ATTACHED(y, z)];
                                                                  \neg \Diamond \mathsf{ATTACHED}(x,y) \land \neg \Diamond \mathsf{SUPPORTS}(x,y) \land
                                                                 SUPPORTS(z, y) \wedge
                                                                  \neg \diamondsuit \text{SUPPORTED}(x) \land \neg \diamondsuit \text{ATTACHED}(y, z) \land
                                                                  \neg \Diamond \text{SUPPORTS}(y, x) \land \neg \Diamond \text{SUPPORTS}(y, z) \land
                                                                  \neg \diamondsuit SUPPORTS(x, z) \land \neg \diamondsuit SUPPORTS(z, x)
                                                      \neg \Diamond z = w \wedge \neg \Diamond z = x \wedge \neg \Diamond z = y \wedge
           STACK(w, x, y, z)
                                                      PUTDOWN(w, x, y) \land \text{SUPPORTS}(z, y) \land \neg \text{ATTACHED}(z, y)
                                                       \neg \Diamond z = w \land \neg \Diamond z = x \land \neg \Diamond z = y \land
      Unstack(w, x, y, z)
                                                      PickUp(w, x, y) \land Supports(z, y) \land \neg Attached(z, y)
            MOVE(w, x, y, z)
                                                  \neg \diamondsuit y = z \land [\text{PickUp}(w, x, y); \text{PutDown}(w, x, z)]
     ASSEMBLE(w, x, y, z)
                                                  PUTDOWN(w, y, z) \land_{\{<\}} STACK(w, x, y, z)
\mathsf{Disassemble}(w,x,y,z) \ \stackrel{\triangle}{=} \ \mathsf{Unstack}(w,x,y,z) \land_{\{<\}} \mathsf{PickUp}(x,y,z)
```



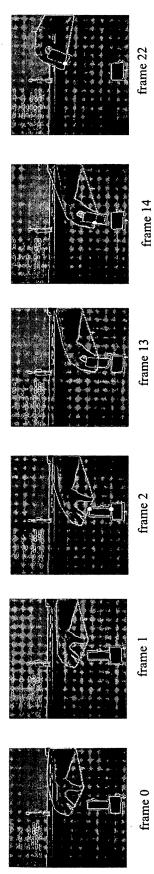


FIG. 5A

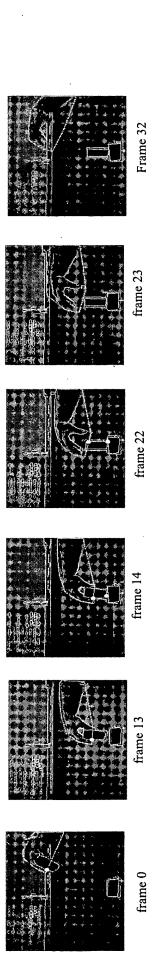


FIG. 5B



```
(PICK-UP MOVING RED GREEN)@([[0,1],[14,22]))

(SUPPORTED? RED)@([[0:22]))
(SUPPORTED? MOVING)@([[1:13]), [[24:26]))
(SUPPORTS? RED MOVING)@([[1:13]), [[24:26]))
(SUPPORTS? MOVING RED)@([[0:14]))
(SUPPORTS? GREEN RED)@([[0:14]))
(SUPPORTS? GREEN MOVING)@([[1:13]))
(CONTACTS? RED GREEN)@([[0:2]), [[6:14]))
(ATTACHED? RED MOVING)@([[1:26]))
(ATTACHED? RED GREEN)@([[1:6]))
```

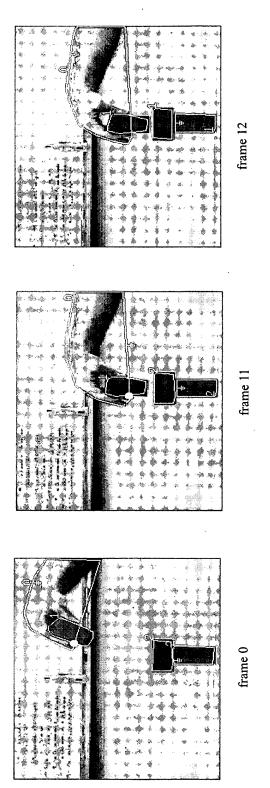
```
(PUT-DOWN MOVING RED GREEN)@([[0,14],[23,32])}

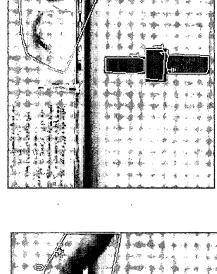
(SUPPORTED? MOVING)@([[14:23])}
(SUPPORTES? RED)@([[0:32])}
(SUPPORTS? MOVING RED)@([[0:14])}
(SUPPORTS? RED MOVING)@([[14:23]))
(SUPPORTS? GREEN MOVING)@([[14:23]))
(SUPPORTS? GREEN RED)@([[14:23]))
(CONTACTS? RED GREEN)@([[22:32]))
(ATTACHED? MOVING RED)@([[0:23]))
(ATTACHED? RED GREEN)@([[14:22]))
```

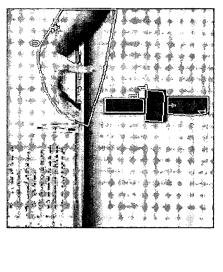
FIG. 6A

FIG. 6B







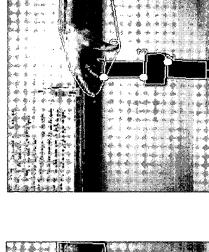


frame 24

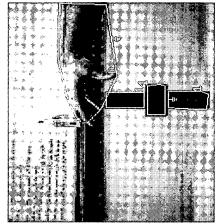
frame 23

FIG. 7A

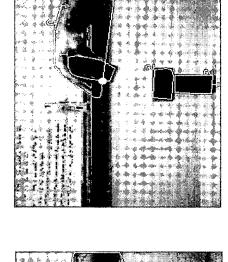




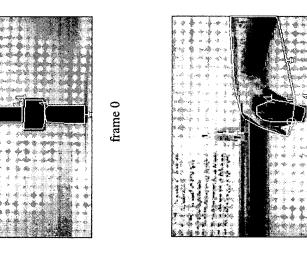




frame 10

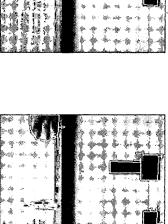


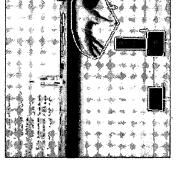
frame 33

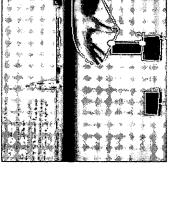


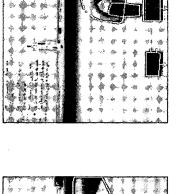
frame 24

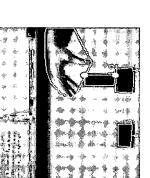
# FIG. 7B











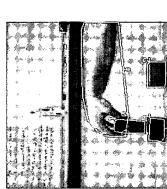


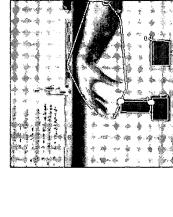
frame 16

frame 9

frame 8

frame 0





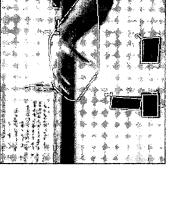


frame 33

frame 17

frame 45

FIG. 7C



frame 52



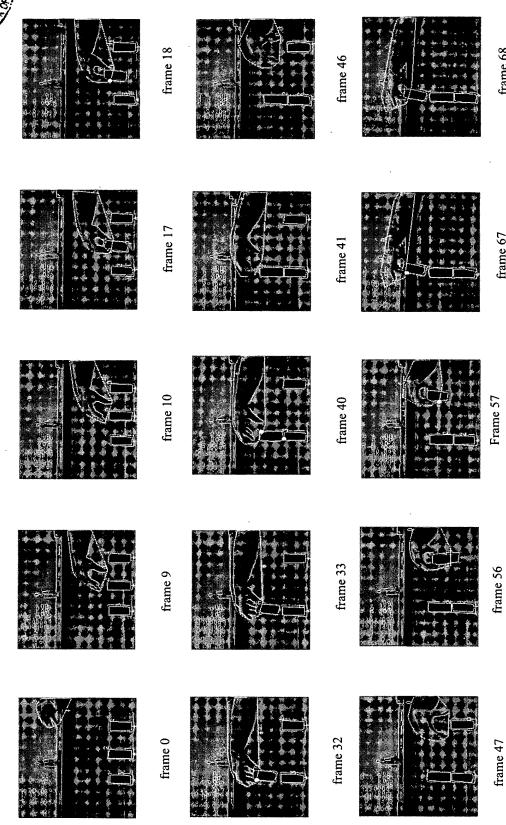


FIG. 7D

frame 68

frame 67



```
(PUT-DOWN HOVING RED BLUE)@([[0,12],[24,30])}
(STACK MOVING RED BLUE GREEN)@([[0,12],[24,30]))

(SUPPORTED? MOVING)@([[13:24])}
(SUPPORTED? RED)@([[0:30]))
(SUPPORTS? RED)@([[0:30]))
(SUPPORTS? RED HOVING)@([[19:20]),
(SUPPORTS? RED HOVING)@([[19:20]),
(SUPPORTS? GREEN HOVING)@([[19:20]),
(SUPPORTS? GREEN BLUE)@([[19:20]),
(SUPPORTS? GREEN BLUE)@([[0:30]))
(SUPPORTS? GREEN BLUE)@([[0:30]))
(SUPPORTS? GREEN BLUE)@([[0:30]))
(SUPPORTS? GREEN BLUE)@([[0:30]))
(SUPPORTS? BLUE RED)@([[19:20]),
(SUPPORTS? CREEN BLUE)@([[0:30]))
(CONTACTS? GREEN BLUE)@([[0:30]))
(ATTACHED? MOVING RED)@([[0:24]))
(ATTACHED? MOVING RED)@([[0:24]))
(ATTACHED? MOVING RED)@([[0:24]))
```

## FIG. 8A

```
(PICK-UP MOVING RED GREEN) @ ([[0.9], [17, 46])}
(PUT-DOWN HOVING RED BLUE)@([[17,35],[46,52]))
(MOVE MOVING RED GREEN BLUE) @([[0,9],[46,52]))
(SUPPORTED? MOVING)@([[9:15])}
(SUPPORTED? RED) 0 ([[0:52]))
(SUPPORTED? BLUE)@([[35:46])}
(SUPPORTS? MOVING RED) @([[17:46])}
(SUPPORTS? MOVING BLUE) 6([(35:46]))
(SUPPORTS? RED MOVING) 6([[9:15]))
(SUPPORTS? RED BLUE) ([[35:46]))
(SUPPORTS? GREEN MOVING) 0([[9:15]))
(SUPPORTS? GREEN RED) @ ([[0:17]))
(SUPPORTS? BLUE RED) 6 ([[46:52]))
(CONTACTS? RED GREEN) 6([[0:17]))
(CONTACTS? RED BLUE) 0 ([[46:52]))
(ATTACHED? MOVING RED) 0 ([[9:46]))
(ATTACHED? RED BLUE)@{[[35:46])}
```

# FIG. 8C

```
(PICK-UP MOVING RED GREEN) 6 ([[0,19],[23,50]))
(PICK-UP MOVING GREEN BLUE)@([[22,58],[62,87])}
(UNSTACK MOVING RED GREEN BLUE)@([[0,19],[23,50]))
(DISASSEMBLE MOVING RED GREEN BLUE) @([[0,19],[62,87]))
(SUPPORTED? MOVING) @([[19:22])) (SUPPORTED? RED) @([[0:50]))
(SUPPORTED? GREEN) @ ([[0:87]))
(SUPPORTED? BLUE) 4{[[58:62])}
(SUPPORTS? MOVING RED) 0 ([[23:50])) (SUPPORTS? MOVING GREEN) 0 ([[58:87]))
(SUPPORTS? MOVING BLUE) 6{[[58:62])}
(SUPPORTS? RED MOVING) 6([[19:22])}
(SUPPORTS? GREEN MOVING)@{[[19:22])}
(SUPPORTS? GREEN RED) @([[0:23])}
(SUPPORTS? GREEN BLUE) @([[58:62]))
(SUPPORTS? BLUE GREEN)@([[0:58])}
(CONTACTS? RED GREEN)@([[0:23])}
(CONTACTS? GREEN BLUE) @([[0:58])}
(ATTACHED? MOVING RED)@([[19:50])}
(ATTACHED? MOVING GREEN)@([[58:87])}
(ATTACHED? GREEN BLUE)@([[58:62])}
```

FIG. 8E

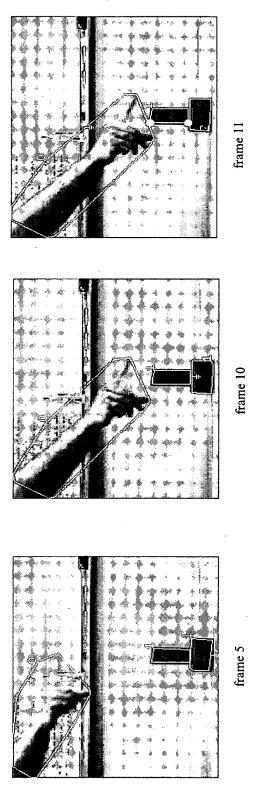
```
(PICK-UP MOVING RED BLUE) @([[0,11],[25,33])}
(UNSTACK MOVING RED BLUE GREEN) 0 ([[0,11], [25,33]))
(SUPPORTED? MOVING) 6([[11:23]))
(SUPPORTED? RED) @([[0:36]))
(SUPPORTED? BLUE) @([[0:36])}
(SUPPORTS? MOVING RED) @([[23:36]))
(SUPPORTS? RED MOVING) 4 ([[11:23]))
(SUPPORTS? RED BLUE)@([[13:14])}
(SUPPORTS? GREEN MOVING)@([[13:14])}
(SUPPORTS? GREEN RED) 6 ([[13:14]))
(SUPPORTS? GREEN BLUE) @ ([(0:36]))
(SUPPORTS? BLUE MOVING) @([[11:23]))
(SUPPORTS? BLUE RED)@([[0:25])}
(CONTACTS? MOVING RED) 0 ([[34:36]))
(CONTACTS? RED BLUE)@([[0:13]), [[14:24])}
(CONTACTS? GREEN BLUE)@([[0:13]), [[14:36])}
(ATTACHED? HOVING RED) @([[11:33]))
(ATTACHED? RED BLUE)@([[13:14]))
(ATTACHED? GREEN BLUE) @([[13:14]))
```

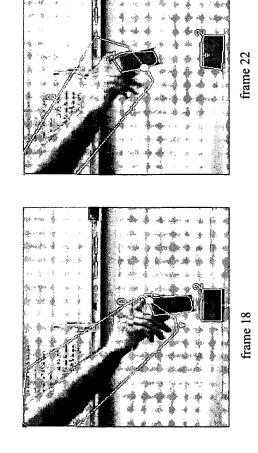
### FIG. 8B

```
(PUT-DOWN MOVING RED GREEN)@([[57,68],[68,87])}
(PUT-DOWN MOVING GREEN BLUE) 0 ([[18,35],[41,47]))
(STACK MOVING RED GREEN BLUE) 0 { [[57,68], [68,87]) }
(ASSEMBLE MOVING RED GREEN BLUE) 6([[18,35],[68,87]))
(SUPPORTED? MOVING) @([[10:18]), [[47:57])}
(SUPPORTED? RED)@([[57:87]))
(SUPPORTED? GREEN)@([[11:87]))
(SUPPORTED? BLUE) 0{[[35:41])}
(SUPPORTS? MOVING RED)@([[57:68]))
(SUPPORTS? MOVING GREEN)@([[11:41])}
(SUPPORTS? MOVING BLUE)@([[35:41]))
(SUPPORTS? RED MOVING)@([[10:18]), [[47:57]))
(SUPPORTS? RED GREEN) 6 ([[11:16]))
(SUPPORTS? GREEN RED) @ ([[68:87]) }
(SUPPORTS? GREEN BLUE) @ ([[35:41]) }
(SUPPORTS? BLUE GREEN)@([[41:87]))
(CONTACTS? RED GREEN) 6([[68:87]))
(CONTACTS? GREEN BLUE)@([[41:87])}
(ATTACHED? MOVING RED)@([[11:16]), [[49:68])}
(ATTACHED? MOVING GREEN)@([[11:41])}
(ATTACHED? GREEN BLUE)@(([35:41]))
```

FIG. 8D







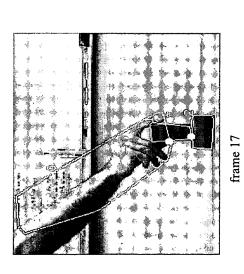


FIG. 9A



(PICK-UP MOVING RED GREEN) 0 ([[0,11],[18,30]))

(SUPPORTED? RED)e([[0:30]))
(SUPPORTED? GREEN)e([[11:18]))
(SUPPORTS? MOVING RED)e([[11:30]))
(SUPPORTS? MOVING GREEN)e([[11:18]))
(SUPPORTS? RED GREEN)e([[11:18]))
(SUPPORTS? GREEN RED)e([[0:11]))
(CONTACTS? RED GREEN)e([[0:11]))
(ATTACHED? MOVING RED)e([[11:30]))
(ATTACHED? RED GREEN)e([[11:30]))

**FIG. 10A** 

FIG. 10B

(PICK-UP MOVING RED GREEN)@{[[0,8],[19,30])}

(SUPPORTS? YELLOW BLUE) &([[0:30]])
(CONTACTS? RED GREEN) &([[0:10]), [[16:19]))
(CONTACTS? BLUE YELLOW) &([[0:30]])

(SUPPORTED? MOVING) @ ([8:19])}

(SUPPORTS? MOVING RED) 0 ([[19:30]))

(SUPPORTS? GREEN MOVING)@{[[8:19])} (SUPPORTS? GREEN RED)@{[[0:19])}

(SUPPORTS? RED MOVING) @ ([[8:19]))

(ATTACHED? MOVING RED)@[[8:30])} (ATTACHED? RED GREEN)@([[10:16])}

(SUPPORTED? RED) @([[0:30])) (SUPPORTED? BLUE) @([[0:30]))

```
(PICK-UP MOVING RED GREEN)@([[52,70],[78,102]), [[0,9],[19,44]))
(PUT-DOWN MOVING RED GREEN)@([[19,44],[62,70]), [[78,102],[110,117]))

(SUPPORTED? MOVING)@([[9:18]), [[44:52]), [[70:77]), [[102:110]))
(SUPPORTS? RED)@([[0:117]))
(SUPPORTS? RED MOVING)@([[9:18]), [[44:52]), [[70:77]), [[102:110]))
(SUPPORTS? GREEN MOVING)@([[9:18]), [[44:52]), [[70:77]), [[102:110]))
(SUPPORTS? GREEN BED)@([[0:19]), [[44:52]), [[70:77]), [[102:110]))
(CONTACTS? RED GREEN)@([[0:19]), [[13:18]), [[46:70]), [[106:117]))
(ATTACHED? MOVING RED)@([[9:52]), [[70:76]), [[104:106]))
```

**FIG. 10C** 

(PICK-UP MOVING RED GREEN) 0 ([[0,6],[16,22])) (PICK-UP MOVING YELLOW BLUE) @ ([[0,12],[17,22])} (SUPPORTED? MOVING) 6 ([[6:16])) (SUPPORTED? MOVING) @ ([12:15])) (SUPPORTED? RED) @ ([[0:22])) (SUPPORTED? YELLOW) @ ([[0:22]) }
(SUPPORTS? MOVING RED) @ ([[16:22]) } (SUPPORTS? MOVING YELLOW) 0{[[17:22])} (SUPPORTS7 RED MOVING) @([[6:16])) (SUPPORTS? GREEN MOVING) @([[6:16])} (SUPPORTS? GREEN RED) @([[0:16])} (SUPPORTS? BLUE MOVING) @ ([[12:15])} (SUPPORTS? BLUE YELLOW) @([[0:17])} (SUPPORTS? YELLOW HOVING) 0([[12:15])) (CONTACTS7 RED GREEN) @([[0:15])} (CONTACTS? RIJE YELLOW) @{[[0:17])} (ATTACHED7 MOVING RED) 0 ([[6:22])) (ATTACHED? HOVING YELLOW) @{[[12:22])}

**FIG. 10D** 



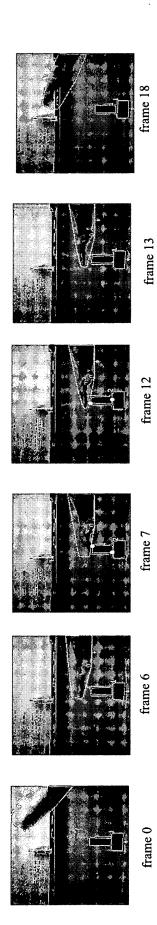


FIG. 11A









frame 21

frame 19

frame 18

frame 12

frame 11

FIG. 11B



(SUPPORTED? RED) 0 ([[0:25]))
(SUPPORTED? GREEN) 0 ([[7:13]))
(SUPPORTS? MOVING RED) 0 ([[7:13]))
(SUPPORTS? MOVING GREEN) 0 ([[7:13]))
(SUPPORTS? RED GREEN) 0 ([[0:7]), [[13:25]))
(CONTACTS? RED GREEN) 0 ([[0:7]), [[13:25]))
(ATTACHED? MOVING RED) 0 ([[7:13]))
(ATTACHED? RED GREEN) 0 ([[7:13]))

(SUPPORTED? RED)@([[0:19]))
(SUPPORTED? MOVING)@([[13:31]))
(SUPPORTS? RED MOVING)@([[13:31]))
(SUPPORTS? MOVING RED)@([[0:13]))
(SUPPORTS? GREEN RED)@([[12:19]))
(SUPPORTS? GREEN MOVING)@([[0:31]))
(ATTACHED? RED MOVING)@([[0:31]))
(ATTACHED? RED GREEN)@([[13:19]))

FIG. 12A

FIG. 12B